9th International Mathematics and Science Olympiad (IMSO) for Primary School 2012

Instructions:

- * Write down your name and country on the answer sheet.
- * Write your answer on the answer sheet.
- * You have 120 minutes to work on this test.
- * Use pen or pencil to write your answer.



"Smart, Skilled, and Creative In a Joyful Competition for Excellence"

City Montessori Inter College, RDSO Campus, Manak Nagar, Lucknow, India 27 Oct. – 2 Nov 2012

International Mathematics and Science Olympiad 2012

EXPLORATION PROBLEMS

1. Fill in the positive integers 1 to 30 into the following boxes to form 15 fractions, with each number used exactly once, such that as many of these fractions as possible have integer values.

| \Box , | \Box , | \Box , | \Box , | $\overline{\Box}$, | \Box |
|----------|----------|----------|----------|---------------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|--------|

- 2. A palindrome number is a positive integer that can be read the same way in either direction. For instance, 909, 3553 and 12421 are palindrome numbers. Find all 5-digit palindrome numbers divisible by 44.
- 3. The plane is divided into a number of non-overlapping polygons by *n* lines. What is the largest number of triangles among these polygons?
 - (a) When n=5? (1 point)
 - (b) When *n*=6? (2 point)
 - (c) When *n*=7? (3 point)
- 4. Select as many of the integers from 1 to 21 as possible, so that no two disjoint pairs of them have the same difference. For example $\{1, 3, 5, 13\}$ is such a collection; although 3-1=5-3, the two pairs are not disjoint. On the other hand, $\{1, 2, 4, 7, 10\}$ is not since 4-1=10-7. What is the maximum number of integers that can be select?
- 5. Find a three-digit number such that the ratio of this three-digit number to the sum of its digit has the least value.
- 6. Place the numbers 1 to 42 in the squares of the 6×7 table so that any two consecutive numbers are in squares which share a common side. The numbers 11, 20 and 30 are already placed as shown in the diagram below.

11	20		
30			

EXPLORATION PROBLEMS

NAME	COUNTRY								
1. Ans	Answer Sheet								
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3.									
(a) (b)	(c)								

EXPLORATION PROBLEMS

NAME _____ COUNTRY _____

Answer Sheet

4. The maximum number of integers that can be selected is ______.

5. The answer is _____.

6.

11	20		
30			